

Full diffraction patterns with a 2θ -range $[5, 120]^\circ$ were measured at 12, 28, 60 and 100 K, as shown in Fig. F.1. Smaller 2θ -range $[42.5, 57]^\circ$ datasets were measured between 20 K and 150 K (36 temperatures). Raw diffraction patterns are shown in Fig. F.2 for selected temperatures. Some peak splittings are observed below 80 K, evidencing a structural transition in VI_3 .

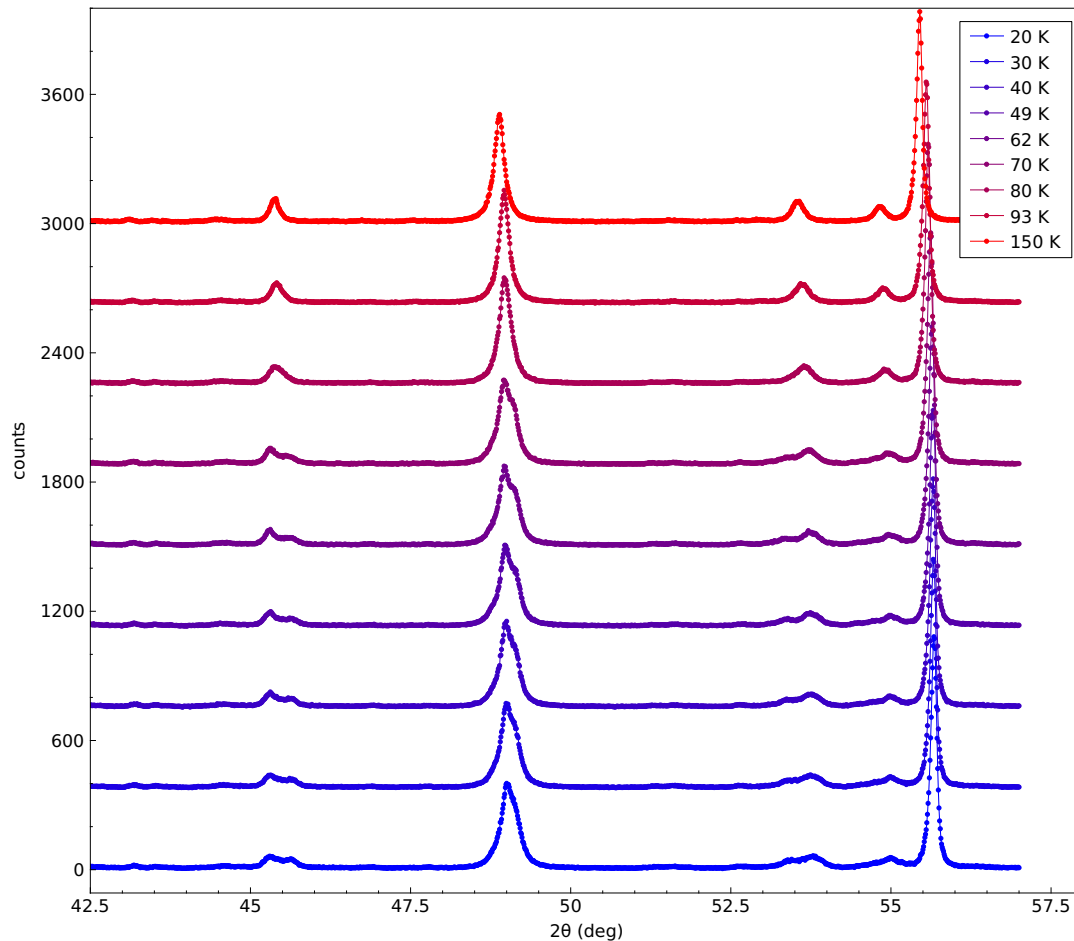


Figure F.2 Stacked plots of the X-ray powder diffraction patterns for selected temperatures.

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